

$$p_n = 1 + \sum_{i=1}^{2^n} \left[\left(\frac{n}{\sum_{j=1}^i \left[\cos^2 \left(\pi \frac{(j-1)!+1}{j} \right) \right] } \right)^{1/n} \right]$$